

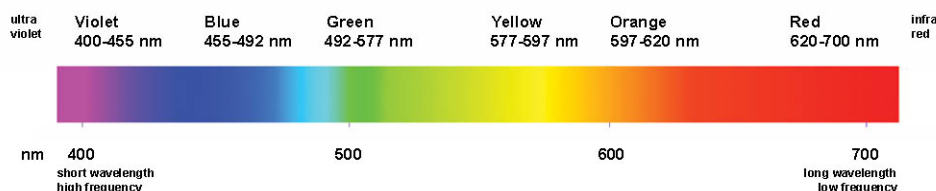
Chem 4A Scholars Worksheet 4

Quantization, Photoelectric Effect and Bohr Atom

Useful equations:

$$E_P = \frac{hc}{\lambda} \quad \nu = \frac{1}{\lambda} \quad E_P = E_K + \phi \quad E_K = \frac{1}{2} m v^2 \quad \nu = -R_\infty \frac{Z^2}{n^2} \quad c = 3.00 \times 10^8 \text{ m s}^{-1}$$

$$h = 6.63 \times 10^{-34} \text{ J s} \quad R_\infty = 10973731.6 \text{ m}^{-1} \quad 1 \text{ eV} = 1.602 \times 10^{-19} \text{ J} \quad m_e = 9.10 \times 10^{-31} \text{ kg}$$



Questions:

1. 700nm light was shine on a Calcium surface. Will electrons be ejected? If so, what is the maximum speed of the electron? $\phi(\text{Ca}) = 1.87 \text{ eV}$

$$\phi(\text{Ca}) = 1.87 \text{ eV} = 1.87 \times 1.602 \times 10^{-19} = 3.00 \times 10^{-19} \text{ J}$$

$$E_P = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \times 3.00 \times 10^8}{7.00 \times 10^{-7}} = 2.84 \times 10^{-19} \text{ J} < \phi(\text{Ca})$$

Electron will not be ejected.

2. What if the wavelength of the incident light is 400nm?

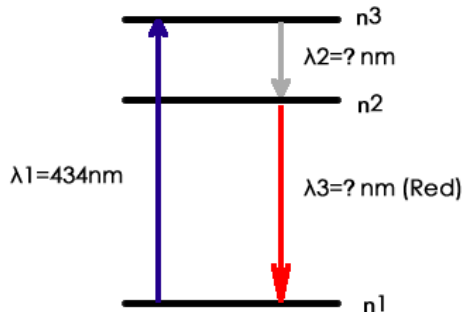
$$E_P = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \times 3.00 \times 10^8}{4.00 \times 10^{-7}} = 4.97 \times 10^{-19} \text{ J} > \phi(\text{Ca})$$

Electron will be ejected.

$$E_k = E_P - \phi = 4.97 \times 10^{-19} - 3.00 \times 10^{-19} = 1.97 \times 10^{-19} \text{ J}$$

$$v = \sqrt{\frac{2 E_k}{m_e}} = \sqrt{\frac{2 \times 1.97 \times 10^{-19}}{9.10 \times 10^{-31}}} = 6.58 \times 10^5 \text{ m s}^{-1}$$

3. Solve the following problem according to the Bohr's model:



A hydrogen atom was initially at some unknown energy level n_1 . The hydrogen atom absorbed a photon with wavelength of 434nm, and went to a higher energy state n_3 . It then went through 2 transitions and emits two photons. The second photon was red. Find the wavelength of the first photon and the second photon was red. Find the energy levels n_1 , n_2 , n_3 , and the wavelength of the photons.

First not that λ_1 is with in the Visible spectrum, which means that it belongs to the Balmer series. $n_1=2$.

$$\frac{1}{\lambda_1} = R_{\infty} \left(\frac{1}{n_1^2} - \frac{1}{n_3^2} \right)$$

$$\frac{1}{434 \times 10^{-9}} = 10973731.6 \times \left(\frac{1}{2^2} - \frac{1}{n_3^2} \right)$$

$$n_3 = 5$$

n_2 can be 3 or 4. When $n_2 = 3$, $\lambda_3 = 656\text{nm}$, which is red.

$$\frac{1}{\lambda_2} = R_{\infty} \left(\frac{1}{n_2^2} - \frac{1}{n_3^2} \right)$$

$$\lambda_2 = 1282\text{nm}$$

4. Would you expect a photon with wavenumber of 30000 cm^{-1} to be absorbed by a hydrogen atom at ground state?

The energy transition of ground state to excited state is

$$\nu = R_{\infty} \left(\frac{1}{1^2} - \frac{1}{2^2} \right) = 8227500\text{m}^{-1} = 82275\text{cm}^{-1}$$

Thus the photon does not have enough energy to excite the hydrogen atom.